Injection: Hadron Beams

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Abstract
The injection process involves placing a particle beam in a circular hadron accelerator or accumulator at the right time, in the correct orbit, with the right phase space parameters, and minimizing beam losses. Injection insertions are among the most complex parts of an accelerator and, if not properly designed, can compromise the beam quality and, in the worst case, cause machine damage. An overview of the main principles and hardware used for single, multturn, and charge exchange injection systems is presented. Common injection errors and their consequences are explained, together with the definition of the machine aperture and the concept of protection devices. Examples of unconventional injection processes are introduced.

Keywords
Single turn; multturn; charge exchange; mismatch; aperture; machine protection.

1 Introduction
The performance of a hadron collider or accumulator depends on the minimum achievable beam size and the maximum storable intensity. The injection process has a strong influence on both these parameters and, if not properly performed, it might downgrade the effective achievement of a machine. Minimization of the beam size involves positioning the injected beam on the right orbit, with the correct timing, and with matched optics parameters with respect to the ring lattice at the injection point. Small injection losses are then a basic requirement for an efficient transfer into a ring and to avoid any risk of beam-induced machine damage.

Different challenges are encountered, depending on the energy of the injected beams. In the low-energy regime (i.e., \( \sim 10 \) MeV for hadrons), the main concern comes from space charge. Particles in a beam feel electromagnetic forces, which are produced by the beam itself. Assuming an unbunched beam, with a uniform charge density and a circular cross-section, each particle will experience an incoherent transverse tune shift \( \Delta Q_{x,y} \) due to space charge, which is proportional to [1]:

\[
\Delta Q_{x,y} \propto \frac{N}{\gamma^2 \beta \varepsilon_N},
\]

where \( N \) is the number of particles per unit length, \( \gamma \) and \( \beta \) the relativistic factors and \( \varepsilon_N \) the r.m.s. normalized transverse emittance. The resulting tune spread can lead to an emittance blow-up and losses. The effect is stronger at low energy and for large energy densities and hence imposes a limit on the maximum achievable brightness.

Injections of \( \sim 100 \) GeV hadron beams are critical because of the large amount of stored energy (up to 2.4 MJ, which is equivalent to 0.5 kg of TNT, for the Large Hadron Collider (LHC) beams) and the consequent disruptive power in the case of wrong handling. A proper choice and correct design of the injection system, which depends on the beam conditions and the main requirements of the receiving machine, enable minimization of the aforementioned undesired effects and thus maximization of the machine performance while guaranteeing the required protection.
2 Single-turn injection

In the ‘single-turn’ injection process, one or more bunches of particles are transferred, all at once, into the receiving ring and, as stated in the label, the procedure is completed in one machine revolution. Each transferred bunch must be injected into an empty RF bucket; this implies that the momentum spread $\Delta p/p$ and the phase $\Delta \phi$ of the incoming beam must be matched to those of the bucket defined by the RF cavity system of the ring [2]. Single-turn injection is performed by bringing the beam onto the central closed orbit of the machine by means of septum magnets [3] and fast deflectors or kickers [4], as shown in Fig. 1. These elements are often installed at each side of a defocusing quadrupole to profit from its additional deflection and hence minimize the strength of the kicker (i.e., the required voltage and the cost of the kicker). The position of the injected beam at the septum $x_s$ must be larger than the sum of both the injected and circulating beam envelopes, taking into account the beam size increase due to the energy spread and the thickness of the septum blade, plus closed-orbit distortions and alignment errors. The injected beam must get an angular deflection $\theta$ from the kicker equal to

$$\theta = \frac{x_s}{\sqrt{\beta_k \beta_s \sin(\mu)}}$$

(2)

where $\beta_k$ and $\beta_s$ are the $\beta$-functions at the kicker and the septum, respectively, and $\mu$ is the relative phase advance between these two elements. Large values of $\beta$ are favourable to reduce the kick angle. Septa can be DC magnetic or electrostatic elements. The leakage into the field-free region of the septa must be adequately shielded to avoid perturbing the circulating beam, in particular at low energy. Different techniques can be used to reduce the stray fields, as explained in Ref. [3].

In general, in an accelerator chain, particles are transferred to rings with larger radius to cope with the increasing rigidity (larger $B \rho$) of the accelerated beams. This allows the accumulation of more bunches at each acceleration stage by several consecutive injections of bunch trains until the receiving machine is filled. The number of bunches that can be stored in a circular accelerator can ideally be defined as the ratio between the ring circumference and the bunch spacing, which is determined by the RF structure. In reality, a number of gaps with no particles must be guaranteed between trains to allow loss-free injections and extractions. Circulating bunches passing through the injection and extraction kickers, when they are pulsing, would be kicked and lost in the machine aperture. Two consecutive trains must be spaced by at least the rise time ($t_{\text{rise}}$) of the injection kickers (as shown in Fig. 2). The so-called abort gap must then be synchronized with the rise time ($t_{\text{abort}}$) of the extraction kickers. As a first
approximation, the number of bunches that can be stored in a ring \( n_b \) can be expressed as

\[
    n_b = \frac{n \cdot t_{\text{flattop}} - \left( (n - 1) \cdot t_{\text{rise}} + t_{\text{abort}} \right)}{t_b},
\]

where \( n \) is the number of injections to fill the ring, \( t_{\text{flattop}} \) is the length of the flat top of the injection kicker waveform, which defines the number of bunches that can be injected at the time (also dependent on the size of the upstream accelerator), and \( t_b \) is the bunch spacing. It is then clear that kickers with fast rise times (from hundreds of nanoseconds up to a few microseconds) are needed to maximize the filling factor that is the ratio between the ideal and the real number of stored bunches.

In ideal conditions, the injected beam should be perfectly superimposed on the closed orbit \((x, x', y, y')\) and fully matched to the optics parameters \((\alpha_{x,y}, \beta_{x,y}, D_{x,y}, D'_{x,y})\) of the ring at the injection point [5]. Errors in the septum or kicker angle, optical mismatch, and inaccurate steering of the transfer lines will lead to an emittance blow-up through filamentation, owing to non-linear effects (e.g., high-order field components), which introduce amplitude-dependant effects to the particle motion [6]. Algorithms, based on the readings from beam position monitors, can be used to identify and correct possible magnetic errors affecting the transfer process and thus minimize the injection oscillations in the receiving machine [7]. This is fundamental to the reduction of both reduce emittance blow-up and injection losses, owing to the interception of particles with large-amplitude oscillations, which represent a potential risk of damage for the machine mechanical aperture.

### 3 Aperture and protection devices

Machine protection becomes one of the largest concerns when dealing with high-energy hadron beams. Failures in the transfer and injection process can occur within a few microseconds and active protection systems (e.g., interlocks, magnet current monitors) might not be able to detect the faults and react in time. In this case, a significant amount of beam can be lost on the machine geometrical aperture \( A_{x,y}^{\text{geom}} \) and, in the worst case, cause damage. Dedicated protection elements are hence installed at specific locations to intercept miskicked beams and protect the accelerator components. The design of a passive protection system starts with the definition of the minimum aperture that these collimators have to shade and protect \( A_{x,y}^{\text{prot}} \), where \( x \) and \( y \) represent the horizontal and vertical plane, see Fig. 3). In particular, they must be set at an aperture \( n_{x,y} \), which, in beam betatron units \((\sigma_{\beta_{x,y}} = \sqrt{\varepsilon_{x,y}/\beta_{x,y}} \text{ with } \varepsilon_{x,y} \text{ r.m.s. geometric emittance})\), is

\[
    n_{x,y} \leq A_{x,y}^{\text{prot}} \leq \min_{s \in [0, L]} \frac{A_{x,y}^{\text{geom}}(s) - \Delta_{x,y}(s)}{\sigma_{\beta_{x,y}}}
\]
Fig. 3: Beam envelope with respect to machine’s geometrical aperture. The injection protection collimators must shadow the aperture of the machine equipment, withstand direct beam impact, and reduce the downstream energy deposition to less than the damage limit.

where \( s \) is the longitudinal co-ordinate along a machine of length \( L \) and \( \Delta_{x,y}(s) \) is the maximum beam transverse displacement:

\[
\Delta_{x,y}(s) = CO_{\text{peak}}^{x,y} \sqrt{\frac{\beta_{x,y}(s)}{\beta_{\text{max}}^{x,y}}} + \left[ \delta_{\text{mech}}^{x,y}(s) + \delta_{\text{align}}^{x,y}(s) \right] + k_p D_{x,y}(s) + d_{\text{sep}}^{x,y}(s) + d_{\text{inj}}^{x,y}(s) + d_{\text{axis}}^{x,y}(s).
\] (5)

In Eq. 5, mechanical (\( \delta_{\text{mech}}^{x,y} \)) and alignment (\( \delta_{\text{align}}^{x,y} \)) tolerances are added to the peak ring closed orbit (CO_{\text{peak}}, which is normalized with respect to the local and the maximum \( \beta \)-functions. A dispersive term is also considered where \( \delta_p \) is the sum of the beam momentum offset and the maximum momentum spread, \( k_p \) is the \( \beta \)-beating correction factor, and \( D_{x,y} \) is the dispersion. The contribution of orbit displacements due to crossing and separation (\( d_{\text{sep}}^{x,y} \)), injection oscillations (\( d_{\text{inj}}^{x,y} \)), and offsets of the magnets with respect to the ring axis (\( d_{\text{axis}}^{x,y} \)) are also taken into account [8]. As a general rule, the higher the beam stored energy, which is defined as the number of particles multiplied by the energy per particle, the larger the margin between the area occupied by the beam and \( A_{\text{geom}}^{x,y} \). Collimators should be set to intercept only miskicked or large-amplitude particles without interfering with the unperturbed injected and circulating beams. Special attention must be used for superconducting machines to limit the number of magnet quenches induced by beam losses.

The passive protection devices must withstand direct beam impacts and reduce energy deposition, owing to secondary showers, on the downstream elements to below the damage limit. The choice of the material of the absorbing blocks and the active length depend on the beam energy and intensity. Low-\( Z \) materials, like graphite, provide the best performance in terms of robustness but are quite transparent to secondary showers. Protection collimators must be set at well-defined longitudinal positions to provide a full coverage of the transverse phase space. As an example, a system of three collimators (each made of two 1 m long graphite jaws) per plane, located at 60° relative phase advance, is installed at the end of the transfer lines connecting the CERN Super Proton Synchrotron (SPS) to the LHC. This layout allows the required phase space coverage to be guaranteed while minimizing the number of collimators (Fig. 4) [9].

A >4 m long two-sided injection dump, composed of a sequence of low- and high-\( Z \) materials [9] to absorb secondary showers, is installed in the LHC injection region at 90° phase advance from the injection kicker. In the case of kicker failures, this dump cuts the particles with the largest amplitudes. The two-sided injection dump will be upgraded to cope with operation with high-brightness beams corresponding to 5 MJ stored energy per injection, which is at the limit of what materials can deal with, in terms of robustness and transmission. Material limitations might constrain the operation of future machines (e.g., the Future Circular Collider (FCC)), limiting the beam intensity that can be transferred at once. This will increase the number of injections required to fill the machine and, therefore, depending on the achievable rise time of the injection and extraction kickers, impact the total stored intensity [10, 11].
**Fig. 4:** Transverse phase space coverage provided by the collimators installed in the SPS-to-LHC transfer line to intercept large-amplitude oscillation particles. These collimators are set at $5\sigma_{\beta_{x,y}}$ to protect the $7.5\sigma_{\beta_{x,y}}$ LHC aperture, assuming a $1.4\sigma_{\beta_{x,y}}$ error in positioning due to alignment or optics errors.

**Fig. 5:** Left: transverse losses mainly occur when largely populated transverse tails of particles are intercepted by aperture bottlenecks, ideally collimators. Right: longitudinal losses are due to ghost low-intensity bunches (grey), located near the main trains (black), which are miskicked by the injection kickers. TDI, two-sided injection dump.

### 4 Injection losses and mitigation

Injection losses are caused by some beam being intercepted at the machine aperture restrictions, which, ideally, correspond to the protection elements. These losses must be controlled and kept as small as possible to prevent damage and minimize the activation of the machine components. Beam losses can be divided into transverse [12] and longitudinal [13] losses (Fig. 5) and detected by means of conventional ionization chambers or diamond beam loss monitors, which are characterized by nanosecond resolutions. Hadron beams can be reasonably well approximated by a transverse Gaussian distribution of particles. The tails of this distribution are often overpopulated and extend well beyond the conventional $3\sigma$. A non-negligible number of particles can then be intercepted by the protection collimators and create losses even during nominal operation without faults. These losses can be minimized through correct steering of the beam in the transfer lines and in the injection region. If this is not sufficient, the beam can be transversely scraped in the pre-injector [14] to remove the tails before the transfer in the next machine. In this case, losses are not suppressed but gathered in dedicated locations, allowing better monitoring and control.

Longitudinal losses occur when, as a consequence of a non-perfect RF capture, some low-intensity
ghost bunches populate the buckets surrounding the main trains. The ghost bunches can be either kicked by the rising or falling edge of the injection kicker magnetic field and lost at the next aperture bottleneck, or be injected on the closed orbit. In the second case, these bunches will be overkicked by the kicker at the next injection and finally lost. If no further tuning of the RF system is possible to mitigate this problem, the ghost bunches can be cleaned by exciting betatron oscillations (i.e., with a transverse damper) until they are lost in dedicated cleaning insertions of the machine.

5 Multiturn injection

Multiturn injection is a process that allows the injection of more bunches into a bucket. This technique is used for hadrons when the beam density at injection is limited by either space charge effects or the injector capacity. When the charge density from the injector cannot be increased, it is possible to fill the horizontal phase space and augment the overall intensity by injecting in the same bucket over several turns [15]. The condition that the acceptance of the receiving machine is larger than the delivered beam emittance must be fulfilled to be able to accumulate intensity via a multiturn injection process. Conventional multiturn injection is performed using a septum and a set of three or four bumpers which, at first, bring the orbit close to the septum blade and then decay in time to zero in a programmed way (Fig. 6). In particular, the bump amplitude is reduced, at each turn, such that the first beam occupies the central region and the later bunches the periphery of the transverse phase space acceptance (Fig. 7). Multiturn injection is often performed in the horizontal plane, owing to the usually larger acceptance. The final particle distribution is defined by the details of the multiturn painting process and by the filamentation, often space charge driven, which finally determines a quasi-uniform charge density. Owing to the finite thickness of the septum blade and the elliptical phase space contours of the injected beam, even in the absence of space charge, the resulting emittance in the receiving machine is

\[ \varepsilon_x > 1.5N\varepsilon_i, \]  

where \( \varepsilon_i \) is the emittance of the injected beam and \( N \) the number of turns over which the injection occurred. Multiturn injection is essential to accumulate high intensity at low energy, when space charge plays a dominant effect. Unfortunately it presents several disadvantages, mainly inherent to the use of the injection septum. The width of the septum blade reduces the available aperture; high losses (up to 30–40%) are produced by the circulating beam hitting the septum and, owing to the limited acceptance, the injection can be performed over a maximum of 10–20 turns.
5.1 Charge exchange

Charge exchange injection provides an elegant alternative to the conventional multiturn injection process [16]. It involves converting $^1_1$H$^-$ ions into protons by using a thin stripping foil, allowing injection in the same phase space area. A decaying magnet chicane is then used to modify the closed-orbit bump and paint the beam uniformly in the transverse phase space (Fig. 8). The thickness of the stripping foils must be carefully chosen to maximize the stripping efficiency, while minimizing emittance blow-up and losses. Typical foils are made of carbon and have a thickness of 50–200 g/cm$^2$ for energies varying between 50 MeV and 800 MeV. The chicane is switched off at the end of the injection, to avoid excessive foil heating and further emittance blow-up. In some cases, longitudinal phase space painting can be performed by varying the energy of the injected beam turn-by-turn, by scaling the voltage of the linac accordingly [17]. A chopper system is then used to match the length of the injected batch to the bucket.

The absence of the septum and the nature of this method allow the injection losses to be reduced to a few per cent. Moreover, the process can continue over tens, up to a hundred, of turns, allowing the accumulation of significant charge densities. Also, in this case, the final particle distribution is determined by the painting and the filamentation due to space charge.

6 Unconventional injection techniques

In the following, examples of unconventional single and multiturn injection techniques are briefly presented.

6.1 Slip stacking

Slip stacking is a configuration that is used to store and accelerate particle beams with different momenta in the same accelerator. This technique was demonstrated for the first time at the SPS to increase the production of anti-protons for $p$–$\bar{p}$ physics [18] and later used at Fermilab for $\bar{p}$ production and to double the power of the proton beam for the target, and, in particular neutrino physics [19]. It involves having two
Fig. 8: The principle of the H\(^-\) charge exchange injection: a magnetic chicane, installed around a thin stripping foil, allows the beam to be painted in the transverse phase space and avoid excessive crossing, which might induce foil heating and emittance blow-up.

Fig. 9: Two sets of bunches slipping in opposite directions and then either (left) combined in the the same RF bucket once azimuthally overlapping or (right) interleaved at an average frequency. Beams \(b_1\) and \(b_2\), which are bunched by two RF cavities with a small frequency difference \(\Delta f = f_2 - f_1\). Each beam is synchronized to one RF cavity (i.e., \(b_1\) to \(f_1\) and \(b_2\) to \(f_2\)) and, at the same time, perturbed by the other (i.e., \(b_1\) by \(f_2\) and \(b_2\) by \(f_1\)). It is possible to define the so-called slip stacking parameter \(\alpha = \Delta f / f_s\), where \(f_s\) is the synchrotron frequency, which determines the level of perturbation felt by each beam due to the presence of the other RF system. When \(\alpha \to 1\), the perturbation is large, while the condition \(\alpha = 4\) corresponds to tangent boundaries for the two stationary buckets, that is, the lower limit for a stable motion. The two sets of bunches drift longitudinally with respect to each other and periodically coincide azimuthally, doubling the local line density (Fig. 9, left). These bunches can then be captured in a common larger bucket with an average frequency \((f_1 + f_2)/2\). The larger the bucket separation (i.e., large \(\alpha\)) the bigger the final emittance due to recombination of the initial set of bunches. The critical point of this technique is to find the correct value of \(\alpha\), which allows enough separation, to limit the mutual perturbation, but, at the same time, minimizes the emittance blow-up.

Studies are ongoing to apply slip stacking in the SPS to increase the number of bunches for operation of the High Luminosity LHC (HL-LHC) with ions [20]. Two super-batches, made of 24 bunches separated by 100 ns, will be injected into the SPS and captured by two pairs of independently controlled 200 MHz cavities. The RF frequency will be varied to accelerate the first batch while decelerating the second one. The two batches will first be let slip and then brought back together by decelerating the first and accelerating the second. Once the bunches are interleaved, they will be recaptured at an average RF frequency (Fig. 9, right). Also, in this case, the final emittance will be blown up, owing to the filamentation of the bunch in the new RF bucket.
6.2 Combined longitudinal and transverse multiturn injection

An accumulation technique that combines multiturn injection and stacking by electron cooling is used in the CERN Low-Energy Ion Ring to increase the number of injected particles [21]. As during conventional multiturn injection, a decreasing closed-orbit bump is used. Injection occurs in a section of the machine characterized by a large normalized dispersion and the energy in the linac is ramped. The bump decrease and the energy ramp are adjusted, such that the instantaneous closed orbit, given by the sum of the bump and the displacement, defined as $D\Delta p/p$, stays constant at injection (Fig. 10). In this way, both the transverse and longitudinal phase space are exploited and injection is performed, keeping the same betatron amplitude but stacking in momentum. Additional stacking in vertical phase space can be performed by using a combination of a magnetic and an inclined electrostatic septum [3]. This implies a complicated geometry of the injection line and additional constraints on the working point to avoid touching the septum blade at each turn. Also, in this case, the injection bump is applied only in the horizontal plane.

The injection of one full pulse from the linac takes approximately $200 \mu s$, corresponding to 76 turns. In total, seven injections are needed to fill the machine and one pulse is injected every $200 ms$, to allow for electron cooling, which takes about 100–150 ms. After each injection, the momentum offset is reduced, through cooling, from 0.4% down to 0.1%; this permits the orbit of the stacked beam to be moved and leaves room for the injection of the next pulse from the linac. Efficiencies of the order of 50–70% are expected with this method.

7 Main lessons

Injections of low-energy beams are dominated by space charge, which makes the storage of high-intensity and high-brightness beams challenging. Conventional multiturn injection with phase space painting allows this limit to be partially overcome but implies a non-negligible emittance growth and large losses at the septum. Moreover, the process is limited to 10–20 turns, owing to the finite acceptance of the receiving machine. Charge exchange H$^-$ injection is an elegant alternative, which permits these limitations to be overcome and high-brightness beams to be produced.

The fast processes involved in the transfer of high-energy beams define a major concern in terms of machine protection. A proper design of the injection insertions and a careful handling of these potentially harmful beams is fundamental. Moreover, the preservation of a small emittance is crucial to maximize the quality of the beam and the machine performance (e.g., the luminosity in a collider). Mismatch and injection errors must be minimized to reduce losses, injection oscillations, and emittance blow-up. Passive protection elements must be installed at strategic locations to reduce the energy deposition on sensitive machine components and avoid damage while limiting activation.
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